

1 **The Influence of Climate State Variables on Atlantic Tropical Cyclone Occurrence**
2 **Rates**

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Abstract

14 We analyzed annual North Atlantic tropical cyclone (TC) counts from 1871-2004,
15 considering three climate state variables—the El Niño/Southern Oscillation (ENSO),
16 peak (Aug-Oct or ‘ASO’) Sea Surface Temperatures (SST) over the main development
17 region (‘MDR’: 6-18° N, 20-60° W), and the North Atlantic Oscillation (NAO)—thought
18 to influence variations in annual TC counts on interannual and longer timescales. The
19 unconditional distribution of TC counts is observed to be inconsistent with the null
20 hypothesis of a fixed rate random (Poisson) process. However, using two different
21 methods, we find that conditioning TC counts on just two climate state variables, ENSO
22 and MDR SST, can account for much or all of the apparent non-random variations over
23 time in TC counts. Based on statistical models of annual Atlantic TC counts developed in
24 this study and current forecasts of climate state variables, we predicted $m=15\pm 4$ total
25 named storms for the 2007 season.

26 **1. Introduction**

27

28 A number of past studies have examined climatic influences on variations at interannual
29 and longer timescales in the occurrence and the intensity of North Atlantic Tropical
30 Cyclones (TCs) [e.g. *Gray*, 1984]. The primary factor considered in past studies is the El
31 Niño/Southern Oscillation (ENSO) [e.g. *Bove et al*, 1998; *Landsea et al*, 1999; *Elsner et*
32 *al*, 2000; *Elsner* 2003; *Elsner et al*, 2006; *Elsner and Jagger*, 2006], though the
33 influence of the North Atlantic Oscillation (“NAO”) has also been examined in some
34 studies [*Elsner et al*, 2000; *Elsner* 2003; *Elsner et al*, 2006; *Elsner and Jagger*, 2006].
35 Both phenomena are believed to influence TC production, development, or prevailing
36 trajectories through their influence on storm tracks or vertical wind shear in the tropical
37 North Atlantic. The ENSO phenomenon tends to enhance (diminish) TC counts during
38 storm seasons coinciding with an incipient La Nina (El Niño) event, while the NAO tends
39 to enhance (diminish) TC counts during storm seasons coinciding with an incipient
40 negative (positive) phase winter. Influences are historically found only during the storm
41 season *preceding* the anomaly in the index; there is no detectable impact on the following
42 year’s storm season.

43

44 Sea Surface Temperatures (SST) over the main development region (‘MDR’: 6-18N, 20-
45 60W) for North Atlantic TCs during the season (Aug-Oct or ‘ASO’) of Peak TC
46 production [*Emanuel*, 2005a; *Webster et al*, 2005; 2006 *Mann and Emanuel*, 2006; *Sriver*
47 *and Huber*, 2006; *Elsner* 2006] have also been argued to be an important influence on
48 long-term North Atlantic TC behavior. MDR SSTs are considered a proxy for potential

49 TC intensity [*Emanuel, 2005a*], with annual TC counts enhanced (diminished) in seasons
50 associated with positive (negative) MDR SST anomalies. Related studies have argued for
51 a significant influence of the so-called “Atlantic Multidecadal Oscillation” (“AMO”) on
52 North Atlantic TC numbers [e.g. *Goldenberg et al, 2001*]. However, as the procedures
53 used to define the “AMO” signal in terms of North Atlantic SSTs in such studies has
54 been challenged in recent work [*Trenberth and Shea, 2006; Mann and Emanuel, 2006*],
55 we have chosen in our analyses here to employ MDR ASO SSTs themselves [as in e.g.
56 *Emanuel, 2005; Mann and Emanuel, 2006; Elsner, 2006*], rather than an index such as
57 the “AMO” derived through statistical processing of the North Atlantic SST field.

58

59 Previous studies have investigated long-term trends in TC statistics [e.g. *Solow and*
60 *Moore, 2000*] or have used regression models employing climatic indices [*Gray 1984;*
61 *Elsner et al, 2000; 2006; Elsner and Jagger, 2006*] and trend parameters [*Elsner 2003*] to
62 predict interannual variations in TC activity. In no previous studies we are aware of,
63 however, have investigators examined whether conditioning on climatic factors can
64 account for the entirety of non-random structure in the statistical distribution of historical
65 North Atlantic annual TC counts. In this study we perform such an examination,
66 employing two distinct and complementary methods to test the hypothesis that annual TC
67 counts follow a state-dependent Poisson process against the null hypothesis of a constant
68 rate Poisson random process.

69

70 Any statistical approach to analyzing TC counts must respect the Poisson distributional
71 nature of the underlying process (that is, that TC counts are characterized by a point

72 process with a low occurrence rate). Our first approach employs Poisson regression [see
73 e.g. *Elsner et al*, 2000; 2001; *Elsner*, 2003; *Elsner and Jagger*, 2006], a variant on linear
74 regression which is appropriate for modeling a conditional Poisson process in which the
75 expected occurrence rate co-varies with some set of state variables (e.g. indices of
76 ENSO, the NAO, and MDR SST). The second approach categorizes the data with
77 respect to the climate state variables using a binary classification scheme, testing both
78 for the statistical significance of differences in occurrence rates between the resulting
79 data subgroups, and examining the resulting subgroup distributions for consistency with a
80 Poisson random process. The two methods are complementary in that the latter method
81 avoids the restrictive linearity assumptions implicit in regression, while the former
82 method accounts for continuous variations in expected TC occurrence rates as a function
83 of the underlying state variables (e.g. distinguishing between the impacts of strong vs.
84 weak El Nino events).

85

86 **2. Data**

87 Our analysis employed four datasets including (1) historical annual North Atlantic TC
88 counts, (2) the Dec-Feb (DJF) Niño3.4 SST ENSO index, (3) the Dec-Mar (DJFM) NAO
89 index, and (4) Aug-Oct (ASO) seasonal SST means over the main development region
90 (“MDR”) of 6°–18°N, 20°–60°W. Our analysis was confined to the 135 year interval
91 1870-2004 over which all three primary datasets of interest were available. The more
92 recent seasons of 2005 and 2006 for which preliminary data are available, are
93 subsequently interpreted in the context of these analyses, while forecasts for the 2007

94 season are made based on projected values of the climate indices. Data are available at
95 the supplementary website: http://www.meteo.psu.edu/~mann/TC_JGR07

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97

98 Historical estimates of the annual TC counts are available back to 1850 [*Jarvinen et al,*
99 2005]. The reliability of these data, particularly prior to the late 20th century in which
100 satellite and aircraft reconnaissance are available, has been vigorously debated in recent
101 studies [e.g. *Landsea, 2005; Emanuel 2005b*]. *Emanuel [2005b]* nonetheless makes a
102 credible argument for why long-term TC count data should be reliable, even if TC
103 intensity estimates are not. As *Emanuel [2005b]* notes, prior to aircraft reconnaissance,
104 ships crossing the Atlantic would not have been warned off from a developing or
105 approaching storm, and were likely to encounter either the storm or evidence of its
106 existence. Combined with other impacts on islands or coastal localities, the existence of
107 an Atlantic tropical cyclone was therefore likely to have been known, even prior to
108 aircraft reconnaissance.

109

110 Various alternative indices of the El Nino/Southern Oscillation (ENSO) are available. We
111 employed the boreal winter (DJF) Niño3.4 index (SST averaged over the region 5°S-5°N,
112 120°-170°W) favored by many investigators [e.g. *Trenberth, 1997*]. Use of alternative
113 (e.g. Niño3) ENSO indices yielded similar conclusions. The Niño3.4 index was taken
114 from the *Kaplan et al [1998]* dataset and updated with subsequent values available
115 through NCEP. The boreal winter (DJFM) NAO index was taken from *Jones et al*
116 [1997], updated with more recent values from the University of East Anglia/CRU. For

117 simplicity, the ‘year’ was defined to apply to the preceding storm season for both indices
118 (e.g. the 1997/1998 El Nino and winter 1997/1998 NAO value were assigned the year
119 1997).

120

121 The MDR SST index was taken from the HadISST2 observational SST dataset [*Rayner et*
122 *al.*, 2003] and updated with more recent values from the UK Met Office. The data were
123 averaged over the season most relevant to tropical cyclone formation (August-September-
124 October, or “ASO”). Estimated uncertainties in the observational SST data are relatively
125 small back to 1870 for both the Nino3.4 and North Atlantic regions of interest in this
126 study [see e.g. *Kaplan et al.*, 1998].

127

128 **3. Methods**

129

130 As in previous studies [e.g. *Elsner et al.*, 2000], we assumed that annual TC counts n can
131 be modeled as a (Poisson) point process, viz.

$$132 \quad P_i(n) = (1/n!) \mu^n \exp(-\mu) \quad (1)$$

133 where the mean occurrence rate μ , is the sole free parameter of the distribution, and in the
134 unconditional case has a Maximum Likelihood value equal to the mean annual count.

135 While the appropriate null hypothesis holds the rate parameter μ to be constant over
136 time, it is of interest to investigate the alternative hypothesis that μ may vary with

137 respect to some set of governing factors or ‘state variables’ [e.g. time—*Solow and*

138 *Moore*, 2000, *Elsner* 2003 and/or climate state indices—e.g. *Elsner*, 2003; *Elsner and*

139 *Jagger*, 2006].

140

141 For the purposes of our study, μ was conditioned on the three climate state variables
142 discussed above (ENSO as measured by the DJF Niño3.4 index, NAO as measured by,
143 the DJFM NAO index, and MDR SST as measured by the MDR ASO SST index). Two
144 distinct statistical approaches were taken, as described below. We note that here is room
145 for further development of the methods presented below. For example, one could extend
146 the approaches used in the present study to account explicitly for the increased
147 uncertainty in TC counts back in time, and in particular the impact of unreported events
148 [e.g. as in *Solow and Moore, 2000; Elsner and Jagger, 2006*].

149

150 *a. Binary Classification Approach*

151 In this approach, each year is classified as belonging to one of two possible binary states
152 (positive or negative) with respect to each state variable, depending on sign of the
153 anomaly in that variable (relative to the 1870-2004 mean). An alternative tertiary
154 classification procedure was tested in which a third neutral category was introduced
155 (defined by absolute anomalies within one standard deviation). The choice of binary vs.
156 tertiary classification schemes represents a tradeoff between the level of discrimination
157 (two vs. three states) and resulting sample sizes. While similar results were obtained
158 using the tertiary categorizations scheme, we preferred the binary classification scheme
159 due to the larger sizes of the data sub-samples. For similar reasons, only the two most
160 significant (see section 4 for further discussion) of the three state variables, MDR SST
161 and Niño3.4 were used.

162

163 Using the binary classification scheme, we categorized years with respect to each of the
164 two factors separately, and further, into three distinct sub-groupings, defined as (1)
165 ‘favorable’: years in which both factors are favorable to TC production (positive MDR
166 SST and negative Niño3.4 anomalies), (2) ‘unfavorable’: years in which both factors are
167 unfavorable to TC production (negative MDR SST and positive Niño3.4 anomalies), and
168 (3) ‘neutral’: years in which the two factors tend to offset in terms of their favorability to
169 TC formation, i.e. anomalies in MDR SST and Niño3.4 that are of the same sign.

170

171 We used a χ^2 test to evaluate the goodness-of-fit of a Poisson distribution for both the
172 unconditional (i.e., all 135 years grouped together) and conditional (i.e., ‘favorable,
173 ‘neutral’, and ‘unfavorable’) data categorizations. We assumed χ^2 to have $v=B-2$ degrees
174 of freedom, where B is the number of occupied bins, and 2 degrees of freedom are
175 subtracted based on constraints provided from the data (normalization of the distribution,
176 and estimation of the rate parameter μ). The bin bandwidth was chosen using the
177 objective criterion cited by *Wilks* [2005],

178
$$h \approx c \text{ IQR} / N^{1/3} \quad (2)$$

179 where N is the sample size, IQR is the inter-fourth quartile range of the data, and $c=2$ is
180 taken for relatively skew distributions such as the Poisson. h was rounded to the nearest
181 integer value.

182

183 The t statistic was then used to evaluate the statistical significance of the differences in
184 TC rate parameter estimates μ_i between any two data sub-samples. The t statistic reduces
185 to

186
$$t = (\mu_1 - \mu_2) / (\mu_1 / \phi_1 + \mu_2 / \phi_2)^{1/2} \quad (3)$$

187 using the expression for the sample variance of a Poisson distribution, $\sigma^2 = \mu$, where
188 ϕ_1 and ϕ_2 denote the degrees of freedom in the respective sub-samples, and the degrees of
189 freedom in the t statistic is $\min(\phi_1, \phi_2) - 1$. When only Niño3.4—which is serially
190 uncorrelated—is used as a conditioning variable, ϕ_1 and ϕ_2 reduce to simply N_1 and N_2 ,
191 the nominal sizes of the respective sub-samples. However, significant serial correlation
192 in the MDR SST series (the lag one autocorrelation coefficient $\rho = 0.55$ yields a
193 decorrelation timescale $\tau = 1.67$ years) decreases the effective number of independent
194 climate states sampled when conditioning on MDR SST as e.g. two neighboring years are
195 not statistically independent with respect to the enhanced likelihood of elevated TC
196 counts. Reduced degrees of freedom (ϕ) were therefore taken into account in estimating
197 the statistical significance of t scores when conditioning fully or partly on the MDR SST
198 series. In such cases, only events spaced more than two decorrelation timescales (i.e., 3
199 years) apart were considered to constitute statistically independent samples.

200

201 Finally, we used a cross-validation procedure to evaluate the predictive skill in the binary
202 conditional Poisson model approach. One could [see e.g. *Elsner and Jagger, 2006*]
203 leave each year out one at a time, forming conditional TC rate parameter estimates based
204 on the remaining years and evaluating the skill of the resulting classifications applied to
205 each choice of missing year. However, when serial correlation is present in the state
206 variables, which as discussed above is the case here, the results of such a cross-validation
207 procedure are likely to give a too liberal an estimate of skill. We therefore employed an
208 alternative split calibration/validation procedure. Conditional TC rate parameter estimates

209 were obtained using the first half (i.e., years 1870-1937) of the data, and subsequently
210 used to categorize the subsequent TC count data based on the climate state variable
211 anomalies (measured relative to the calibration period baseline) over the latter half (i.e.,
212 years 1943-2004). This procedure was then repeated with the role of the first and last half
213 of the datasets reversed. The average of the mean-squared error (MSE) between the
214 predicted and observed TC count data obtained for both sub-intervals was used as an
215 estimate of cross-validated MSE, which was compared to the MSE obtained over the full
216 (1870-2004) model development interval.

217

218 *b. Poisson Regression*

219 Poisson regression is a variant on linear regression appropriate for data such as TC counts
220 for which the null hypothesis of a Poisson distribution is appropriate [see *Elsner et al*,
221 2000; 2001; *Elsner*, 2003; *Elsner and Jagger*, 2006 for further discussion]. Given a count
222 series Y with unconditional mean rate μ believed to follow a state-dependent Poisson
223 distribution, Poisson regression estimates a generalized linear model for the conditional
224 expected rate of occurrence $\lambda = E(Y)$ as a function of a set of state variables X_1, X_2, \dots, X_M ,
225 of the form,

$$226 \quad \log \lambda = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_M X_M \quad (4)$$

227 or alternatively,

$$228 \quad \lambda = \exp[\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_M X_M] \quad (5)$$

229 where the residuals are assumed to be Poisson distributed.

230

231 Unlike ordinary linear regression, a closed-form analytical solution to eq. 5 is not
232 possible. However, it is straightforward to numerically estimate maximum likelihood
233 values for the regression parameters β_i , and thus an estimate for the conditional expected
234 occurrence rates λ_i . The residual series $\varepsilon_i = Y_i - \lambda_i + \mu$ can be analyzed for consistency
235 with a Poisson distribution based on a χ^2 test, as described in section ‘a’ above.

236

237 Poisson regression was performed for various combinations of climate state variables as
238 discussed in more detail in section 4. Cross-validation was performed using the split
239 calibration/validation procedure discussed in section ‘a’ wherein the regressions were
240 performed alternatively using the first and last half of the full data set, with TC counts
241 predicted and compared with observed counts over the remaining independent half of the
242 data set. Quality of regression fit was measured by both the coefficient of determination
243 R^2 and mean square error (MSE).

244

245 **4. Results**

246

247 Certain relationships between annual TC counts and the Niño3.4 and MDR SST time
248 series are evident by inspection alone (Figure 1). The clear increase in TC counts
249 subsequent to the 1920s, and the positive trend over roughly the past decade, closely
250 coincide with corresponding tendencies for positive MDR SST anomalies. Anomalously
251 low TC counts in certain years (e.g. 1982 and 1997) correspond to prominent El Niño
252 years, and the low TC counts of the early 1990s correspond to general tendency for El
253 Niño-like conditions. The NAO has a weaker, but nonetheless statistically significant

254 impact on TC counts, with a tendency for elevation of counts during negative NAO years.
255 The Pearson correlation coefficients between the TC counts and the three predictors
256 ($r=0.48$ for MDR SST, $r=-0.32$ for Niño3.4, and $r=-0.25$) are statistically significant at
257 the $p<0.0001$, $p=0.0001$, and $p=0.003$ levels respectively for a two-sided hypothesis test,
258 taking into account the serial correlation in each series. The extent to which these state
259 variables can account for the non-random structure in long-term TC counts is investigated
260 below using each of the two methods discussed in section 3.

261

262 *a. Binary Classification Approach*

263 We first note that the unconditional distribution of TC counts is highly inconsistent with
264 the null hypothesis of a random Poisson process. Based on a χ^2 test (Table 1) we reject at
265 the $p<0.05$ level the null hypothesis of a Poisson process for the entire TC count record
266 1870-2004. By inspection (Figure 3, panel *a*), it is clear that there is bimodality in the
267 distribution which cannot be captured by the model of a constant mean Poisson process.

268

269 Conditioning on ENSO influences (i.e. on Niño3.4) alone does not ameliorate this
270 problem, as the conditional distributions for negative Niño3.4 values (i.e. ‘La Nina’-like
271 behavior) is still observed (Table 1) to be inconsistent ($p<0.05$) with a Poisson
272 distribution. Conditioning on MDR SST provides significant improvement, though the p
273 values ($p=0.79$ and $p=0.25$ for +MDR SST and –MDR SST respectively) average only
274 just above the median ($p=0.5$) level between acceptance and rejection of the null
275 hypothesis. However, when TC counts are simultaneously conditioned on both Niño3.4
276 and MDR SST, we find that the null hypothesis can likely not be rejected. The resulting

277 three separate distributions ('favorable', 'neutral', and 'unfavorable', as defined in
278 section 3a) are generally well captured by a Poisson distribution (Figure 3, panels *b-d*).
279 While in one of the three cases ('favorable') the p value ($p=0.27$) indicates a moderate
280 27% chance of falsely rejecting the null hypothesis, the χ^2 tests yield an average value
281 $p=0.70$ for the three cases, well above the median expected level for false rejection of the
282 null hypothesis. The results of the analysis are therefore consistent with the hypothesis
283 that the annual TC counts are produced by a state-dependent Poisson process, with the
284 occurrence rate being dictated by two state variables (Niño3.4 and MDR SST).
285
286 Having established the viability of a state-dependent Poisson random model for the
287 observed TC count data, we assessed the statistical significance of differences in the
288 estimated conditional occurrence rates μ . There is a clear dependence of μ both on each
289 of the two state variables separately and on the sub-categorization into the three
290 'favorable', 'neutral', and 'unfavorable' cases (Table 2). The highest average annual TC
291 count is found for the 'favorable' state ($\mu \approx 11$), while the lowest ($\mu \approx 6$) is found for the
292 'unfavorable' state, with all other sub-groupings yielding intermediate values of μ . While
293 differences in occurrence rate (Table 3) are highly significant conditioning on either one
294 of the two state variables (Niño3.4 or MDR SST) alone, the most significant difference
295 (i.e., lowest p value) is observed conditioning on both state variables (i.e., the
296 'unfavorable' vs. 'favorable' categories). Partitioning into the 'favorable', 'neutral', and
297 'unfavorable' categories yields both individual distributions that as noted earlier are on
298 average consistent with Poisson, and mean TC occurrence rates that differ significantly
299 between any two categories (Table 3). The MSE (Table 4) using the conditional means

300 from the binary classification approach (MSE=10.80 for the full 1870-2004 model
301 development interval, and MSE=11.79 in cross-validation) represents a significant
302 improvement over climatology (MSE=13.75) or persistence (MSE=19.89). The cross-
303 validation results, however, suggest that the binary classification approach gives
304 moderately less predictive skill than the Poisson regression approach, as discussed in
305 more detail below.

306

307 *b. Poisson Regression*

308 We performed univariate Poisson regression alternatively using (i) MDR SST and (ii)
309 Niño3.4 as state variables, (iii) bivariate regression using both MDR SST and Niño3.4 as
310 state variables, and (iv) multivariate regression using all three climate state variables
311 MDR SST, Niño3.4, and NAO (Figure 3a). Cross-validated resolved variance R^2 and
312 MSE scores were similar to the scores obtained from the full model development interval
313 1870-2004, and far superior to either climatology or persistence, indicating significant
314 skill in each of the regression models. Interestingly, the predictive skill systematically
315 increases while the consistency of residuals (see Figure 3b) with a Poisson distribution
316 decreases as additional state variables are added to the regression—i.e., first MDR only,
317 then MDR and Niño3.4, and finally MDR, Niño3.4 and NAO (Table 4). Improved skill
318 thus appears to come at a cost of increased bias in the conditional TC rate estimates.

319

320 Each of the Poisson regression models are seen to improve significantly (as measured by
321 both full 1870-2004 model development interval and cross-validation MSE scores) over
322 climatology (Table 4). Moreover, both bivariate and three variable Poisson regression

323 models yield significant improvements (as measured by MSE scores) over the binary
324 classification approach with MDR SST and Niño3 outlined in section 4a. This further
325 suggests a tendency for a tradeoff between resolved variance (as determined from
326 regression and validation R^2 and MSE scores) and bias (as determined from the
327 distribution of residuals) in modeling TC counts. While the binary classification
328 approach yielded the greatest consistency with a pure state-dependent Poisson process (as
329 conditional distributions were consistent with Poisson at a mean level $p=0.70$), it also
330 produced the least resolved variance in modeling annual TC counts by conditioning on
331 two or more climate state variables.

332
333 *c. Predictions*

334 The binary classification approach to modeling TC numbers yields a simple forecasting
335 scheme for seasonal TC counts. Depending on the forecast values for the two state
336 variables (MDR ASO SST and DJF Niño3.4 anomalies) at the start of the tropical
337 cyclone season (June 1st), the predicted TC total would be $\mu=6\pm3$ (i.e., between 3 and 9)
338 for ‘unfavorable’ anomaly combinations, $\mu=9\pm3$ (between 6 and 12) for ‘neutral’
339 anomaly combinations, and $\mu=11\pm3$ (between 8 and 14) for ‘favorable’ anomaly
340 combinations. It is instructive to interpret the two most recent (2005 and 2006) Atlantic
341 tropical storm seasons in this context. The TC count for the 2006 season ($n=10$) was
342 consistent with the predicted count ($m=9\pm3$) given the observed ‘neutral’ conditions
343 (positive MDR SST anomaly and positive 2006/2007 DJF Niño3.4 anomaly—see Table
344 5). The 2005 TC count ($n=28$) is considerably more difficult to explain, even given the
345 ‘favorable’ (positive 2005 MDR SST and negative 2005/2006 DJF Niño3.4) observed

346 conditions, for which the predicted count is $m=11\pm3$. Given a mean expected rate $\mu=11$,
347 the probability of equaling or exceeding a TC count of $n=28$ is $\approx 0.01\%$, i.e. implausible.

348

349 The Poisson regression models all successfully predict the 2006 TC count within
350 estimated uncertainties, but like the binary classification approach, all significantly
351 under-predict the historic 2005 TC total of $n=28$ storms (Table 5, and also Figure 3a).
352 However, the most skillful of the Poisson regression models as judged by cross-
353 validation results (i.e., Table 3)—the three state variable model—comes closest to the
354 observed total with a predicted TC count of $m=18\pm4$. The high predicted total in this
355 case is a result of simultaneously favorable conditions in all three state variables
356 (anomalously warm MDR ASO SSTs, La Nina conditions in the tropical Pacific, and a
357 substantially negative phase NAO). Given a conditional expected mean rate $\mu=18$, the
358 probability of observing or exceeding $n=28$ storms is approximately 2%. In other words,
359 for every 50 years with conditions similar to those observed for 2005, a TC count as high
360 or higher than that observed might be expected given the three variable Poisson
361 regression model. In this case, the 2005 TC total is still observed to be improbable, but
362 not entirely implausible. It is of course possible that the true distribution of TC
363 occurrence is heavy-tailed, in which case the probability of very large counts might be
364 substantially greater than estimated under the assumption of conditional Poisson
365 statistics. One could conceivably also argue that biases in the earlier data [e.g., *Landsea*,
366 2005] leads to an underestimation of the frequency of very large annual counts such as
367 observed in 2005. However, our finding in section a that long-term TC data are
368 essentially consistent with random Poisson statistics after controlling for dependence on

369 two climate state variables, would seem to argue against the proposition that systematic
370 biases compromise the reliability of the earlier data [*Landsea, 2005*].

371

372 Finally, we use the statistical models developed above to forecast Atlantic TC counts for
373 the 2007 tropical storm season. At the time this manuscript was finalized, weak La Nina
374 conditions (Nino3.4 = -0.2) were predicted by NCEP for winter 2007/2008. MDR SST
375 anomalies were currently similar to those observed for the 2005 season, so we infer by
376 persistence ASO MDR SST anomalies equal to those for the 2005 season. As there is no
377 basis for forecasting the winter 2007/2008 NAO value, we assume climatological mean
378 DJFM conditions (NAO index=0.47). Given these assumed values, the binary
379 classification approach yields the ‘favorable’ forecast $m=11\pm3$, while each of the Poisson
380 regression models (with the exception of the Niño3.4-only regression which yields a
381 forecast $m=11\pm3$) predict a total of $m=15\pm4$ storms for the 2007 tropical storm season.

382

383 **5. Conclusions**

384

385 Two different methods, a binary classification scheme and Poisson regression, are used to
386 condition expected annual TC counts on climate state variables. Modeling annual
387 Atlantic TC counts as a state-dependent Poisson process using the binary classification
388 approach, we find that two climatic factors, ENSO and tropical North Atlantic MDR
389 SST, are adequate to explain the apparent non-random variability in historical variations
390 in Atlantic TC numbers. Modeling TC counts instead using Poisson regression, we find
391 that the most skillful statistical model employs all three state variables considered in the
392 study, ENSO, tropical North Atlantic MDR SST, and the NAO, as predictors. This three

393 variable statistical model also comes closest to predicting the historic 2005 TC count of
394 18, ascribing unlike the other statistical models developed in this study, a non-trivial
395 probability for that event given the climate state of 2005. However, analysis of residuals
396 also indicates some evidence of bias, implying the need for cautious use of the model.
397 Three of the four Poisson regression models developed in the study predict 15 ± 4 storms
398 for the 2007 Atlantic tropical storm season.

399

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401

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405

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487 **TABLE CAPTIONS**

488

489

490 **Table 1.** Results of reduced χ^2 tests described in text. Indicated are reduced χ^2 value

491 (χ^2/ν) , degrees of freedom ν and the p value for rejection of the null hypothesis of a

492 Poisson distribution.

493

494 **Table 2.** Estimates of occurrence rate μ for the various TC data sub-groupings discussed

495 in text. Provided are the sample sizes N and, where appropriate, the effective sample size

496 ϕ accounting for temporal autocorrelation in state variables.

497

498 **Table 3.** Results of t tests for differences of occurrence rates μ among the different sub-

499 groupings discussed in text. Indicated are the effective degrees of freedom in the t

500 statistic $\Phi = \min(\phi_1, \phi_2) - 1$, and the one-tailed p value for rejection of the null hypothesis of

501 equal means.

502

503 **Table 4.** Assessments of predictive skill for competing statistical models considered in

504 this study. Mean square error (MSE) over the full model development period (1870-

505 2004) is indicated for each case. The MSE for simple (i) climatological mean and (ii)

506 persistence predictions is provided for comparison. In the case of Poisson regression

507 models, the coefficient of determination (R^2) is also provided. Validation MSE and R^2

508 scores are based on the split calibration/validation procedures described in the text.

509

510 **Table 5.** Climate state variable values and associated annual TC count predictions m and
511 associated one standard error uncertainties $\pm \sqrt{m}$ for 2005-2007. 2007 climate variables
512 are forecast based on the procedure described in the text.

513 **FIGURE CAPTIONS**
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515

516 **Figure 1.** Time Series (1870-2004) of (a) annual Atlantic TC counts, (b) MDR ASO SST
517 time series, (c) Niño3.4 DJF SST index, and (d) NAO DJFM SLP index. Red (blue)
518 indicates positive (negative) anomalies in TC counts and Hurricane-favorable
519 (unfavorable) conditions in the three indices (MDR SST, Niño3.4 and NAO). Note that
520 year convention applies to the ‘D’ in DJF and DJFM for both ‘c’ and ‘d’.

521
522 **Figure 2.** Histograms of TC counts n vs. bin centers (blue) with associated one standard
523 deviation uncertainties ($\pm\sqrt{n}$, yellow shading) and best-fit Poisson distributions (red).
524 Results are shown for unconditional case (all data—panel *a*) and the ‘favorable’, ‘neutral’,
525 and ‘unfavorable’ sub-groupings discussed in the text (panels *b-d*). Bin bandwidths were
526 determined as discussed in text.

527
528 **Figure 3.** Poisson regression models of annual Atlantic TC counts using the MDR ASO
529 SST, Niño3.4, and NAO series as predictors. Shown are (a) the statistical model fits over
530 1870-2004 based on the two univariate, bivariate and three-variable Poisson regressions
531 (colored curves) along with the observed TC counts for 1870-2004 (black curve),
532 observed TC counts for 2005 and 2006 (filled black circles), predicted TC counts for
533 2005 and 2006 (unfilled colored symbols) and 2007 (filled colored symbols). (b) Poisson
534 regression residuals as defined in text (colored curves) along with the observed TC
535 counts for 1870-2004 (black curve).

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Table 1

Scenario (1870-2004)	χ^2/ν	ν	p
All Years	2.09	9	0.027
+MDR SST	0.59	8	0.79
-MDR SST	1.32	3	0.25
+Nino3.4	1.02	8	0.42
-Nino3.4	2.29	7	0.025
+MDR/-Nino ('Favorable')	1.27	6	0.27
-MDR/+Nino ('Unfavorable')	0.28	9	0.98
+MDR/+Nino or -MDR/-Nino ('Neutral')	0.49	7	0.85

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Table 2

Scenario (1870-2004)	μ	N	ϕ
All Years	8.85	135	
+MDR SST	10.33	64	28
-MDR SST	7.52	71	31
+Nino3.4	7.78	58	
-Nino3.4	9.66	77	
+Nino/+MDR ('Favorable')	10.94	35	20
-MDR/+Nino ('Unfavorable')	5.97	29	20
+MDR/+Nino or -MDR/-Nino ('Neutral')	9	71	33

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Table 3

Scenario (1870-2004)	t	Φ	p
+MDR SST vs. -MDR SST	3.59	27	0.0006
+Nino3.4 vs. -Nino3.4	3.70	57	0.0002
Favorable vs. Unfavorable	5.41	19	< 0.0001
Favorable vs. Neutral	2.15	19	0.02
Neutral vs. Unfavorable	4.02	19	0.0004

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548 Table 4
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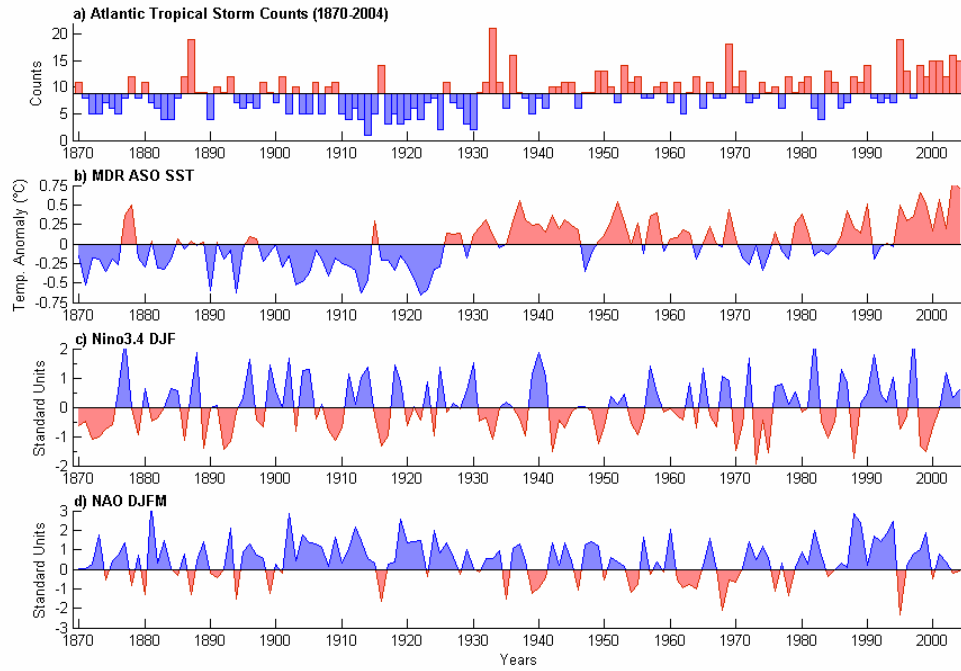
Model/Predictors	<i>R</i>² full	<i>MSE</i> full	<i>R</i>² valid.	<i>MSE</i> valid	<i>p</i> resid.
Climatology	0.00	13.75			
Persistence	0.07	19.89			
Binary Cond: MDR,Nino		10.80		11.79	
Poisson Reg: MDR	0.24	10.81	0.16	10.47	0.83
Poisson Reg: Nino	0.10	12.51	0.12	12.31	0.08
Poisson Reg: MDR,Nino	0.33	9.37	0.26	9.95	0.35
Poisson Reg: MDR, Nino,NAO	0.38	8.70	0.32	9.02	0.00

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Table 5

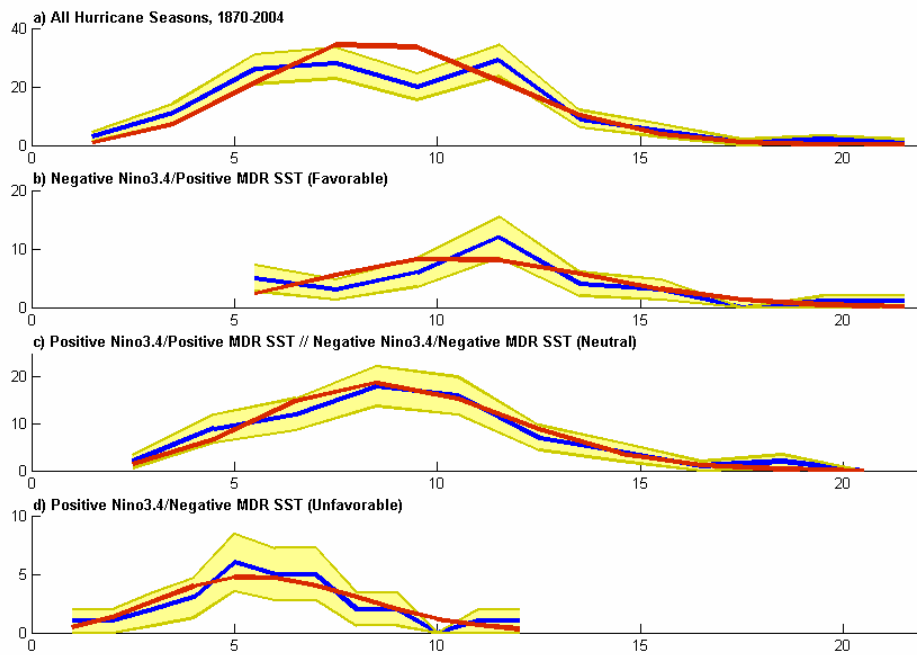
year	model	MDR	Nino3.4	NAO	predicted (<i>n</i>)	observed (<i>m</i>)
2005	Binary Conditioning	+	-	x	<i>11±3</i>	<i>28</i>
	Poisson Regression	x	-0.65	x	<i>10±3</i>	
		28.87C	x	x	<i>15±4</i>	
		28.87C	-0.65	x	<i>16±4</i>	
		28.87C	-0.65	-0.82	<i>18±4</i>	
2006	Binary Conditioning	+	+	x	<i>9±3</i>	<i>10</i>
	Poisson Regression	x	0.72	x	<i>8±3</i>	
		28.35C	x	x	<i>10±3</i>	
		28.35C	0.72	x	<i>9±3</i>	
		28.35C	0.72	2.43	<i>8±3</i>	
2007	Binary Conditioning	+	-	x	<i>11±3</i>	<i>To be determined</i>
	Poisson Regression	x	-0.2*	x	<i>10±3</i>	
		27.9C*	x	x	<i>15±4</i>	
		27.9C*	-0.2*	x	<i>15±4</i>	
		27.9C*	-0.2*	0.47*	<i>15±4</i>	

555 *predicted value
556



558
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FIGURE 1



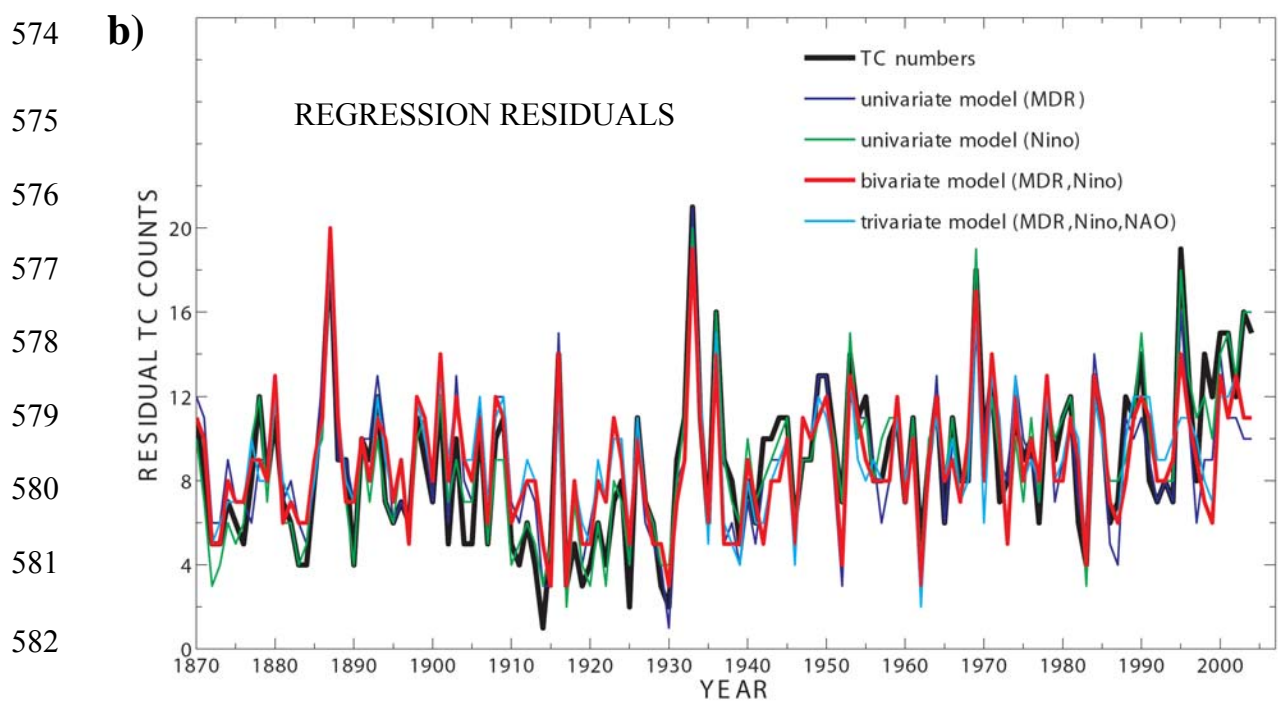
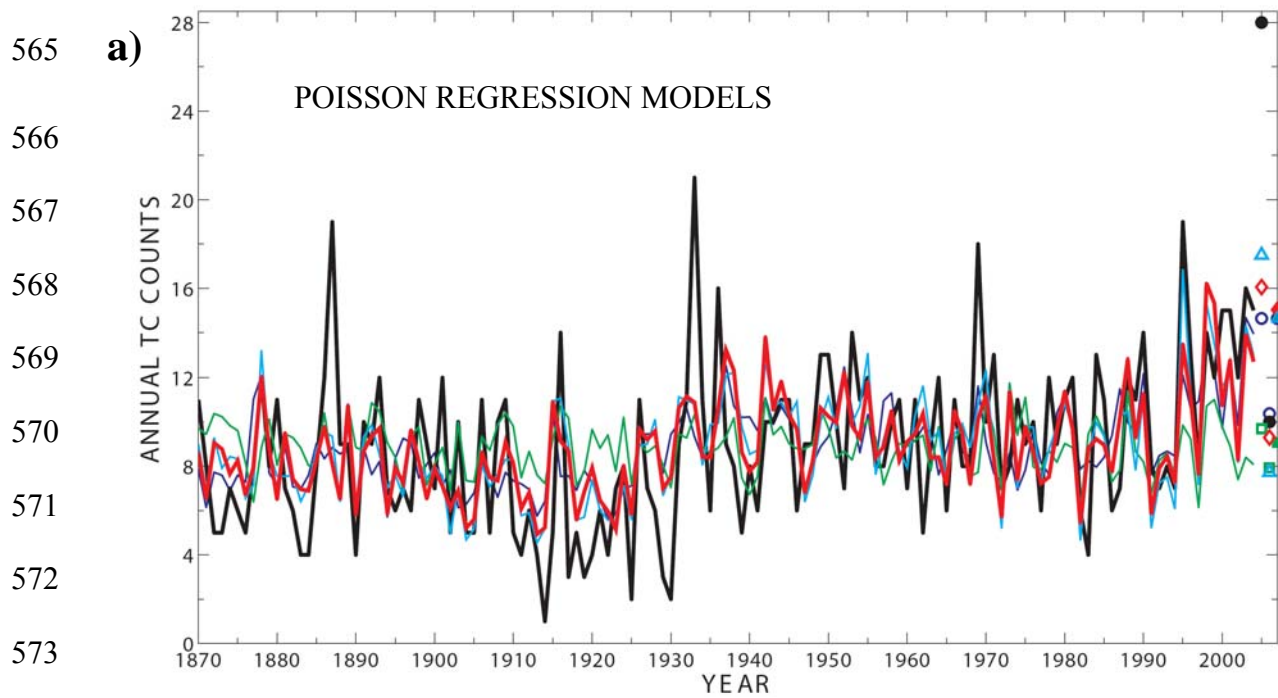
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FIGURE 2

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584 **FIGURE 3**

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