NOTES AND CORRESPONDENCE

A Simulation of a Supercell Thunderstorm with Emulated Radiative Cooling beneath the Anvil

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(Manuscript received 10 September 2004, in final form 20 December 2004)

ABSTRACT

This note reports the preliminary results of an ongoing numerical study designed to investigate what effects, if any, radiative transfer processes can have on the evolution of convective storms. A pair of idealized three-dimensional simulations are conducted to demonstrate the potential dynamical importance of shortwave radiation reductions within the large shadows cast by storms. One of the simulations (the control) is run without surface physics and radiation. In the other simulation, radiative cooling due to cloud shading is emulated by prescribing a cooling rate to the skin temperature at any grid point at which cloud water was present overhead. The imposed skin cooling rate is consistent with past observations. Low-level air temperatures are coupled to the skin cooling in this second simulation by the inclusion of surface sensible heat fluxes using simple bulk aerodynamic drag laws (latent and soil heat fluxes are not included). Significant differences are observed between the two simulated storms, particularly in the evolution of the vertical vorticity field and gust fronts. The storm simulated with emulated cloud shading develops substantially weaker low-level rotation than the storm in the control simulation.

1. Introduction

In this note, we present the preliminary results of an ongoing investigation of the effects of radiative transfer processes associated with long-lived convective storms on storm dynamics. This paper summarizes the outcome of a three-dimensional numerical simulation of a supercell thunderstorm in which cloud shading has been crudely parameterized. Surface cooling due to the cloud shading modifies the low-level temperature field, and these modifications, in turn, alter the storm kinematic fields in significant ways. A review of pertinent past research is presented in section 2. Section 3 describes the design of the numerical experiment and summarizes the results. Section 4 contains a discussion of the results. Finally, some comments on the future work that is planned in this study appear in section 5.

2. Motivation

a. Long-lived convective storms and radiative transfer processes

Long-lived convective storms tend to be among the storms most likely to produce severe weather, such as flash floods, destructive straight-line winds, hail, and tornadoes. For this reason, long-lived storms, such as supercell thunderstorms and mesoscale convective systems (MCSs), have been some of the most intensely studied forms of atmospheric convection. Consequently, these types of storms are perhaps better understood than less severe forms of convection. For example, considerable dynamical insight into supercell thunderstorms (e.g., the dynamics of storm propagation and the origins of midlevel storm rotation) was acquired once computing power became sufficient for the three-dimensional numerical simulation of such storms in roughly the mid-1970s (Schlesinger 1975; Klemp and Wilhelmson 1978a,b; Wilhelmson and Klemp 1978; Rotunno and Klemp 1982, 1985; Klemp and Rotunno 1983; Weisman and Klemp 1982, 1984). Although many observational studies have provided a foundation for...
our current understanding of MCSs (Newton and Fankhauser 1964; Houze 1977; Zipser 1977; Maddox 1980), numerical simulations also have been indispensable in augmenting our comprehension of these larger-scale thunderstorm conglomerations (Hane 1973; Thorpe et al. 1982; Rotunno et al. 1988; Weisman et al. 1988; Fovell and Ogura 1988).

Even though numerical simulations often have produced convective storms that closely resemble those that have been observed, a potentially important forcing has frequently been ignored in these simulations—the influence of radiative effects on storm dynamics. Virtually all of today’s mesoscale weather prediction models include radiation parameterizations, in addition to representations of the other components of the surface energy budget, but the representation of the surface energy budget in numerical simulations of convective storms done for research purposes has been far from commonplace, perhaps in the interest of limiting the studies to the essential dynamics.

It is true that some two-dimensional numerical studies of MCSs have previously included longwave radiative transfer processes. For example, it has been shown that the formation of the well-documented transition zone in MCSs (Small and Houze 1985; Rutledge and Houze 1987; Biggerstaff and Houze 1993) can be sensitive to longwave radiation (Chen and Cotton 1988; Chin 1994; Braun et al. 1996). Furthermore, longwave radiation effects are known to affect the circulation within the trailing stratiform regions of simulated MCSs (Chen and Cotton 1988; Dudhia 1989; Churchill and Houze 1991; Tao et al. 1991), ultimately enhancing precipitation amounts within the stratiform regions (Tao et al. 1993), which typically account for a significant fraction (up to 50%) of the total precipitation produced by MCSs (Houze 1977; Zipser et al. 1981; Gamanche and Houze 1983; Rutledge and Houze 1987; Johnson and Hamilton 1988). Although the studies cited above have made important contributions toward our understanding of MCSs, the full range of possible dynamical effects owing to radiative effects, especially those owing to shortwave radiative transfer processes, remains uncertain due to the model dimensionality of these previous studies. In three-dimensional numerical simulations of MCSs (e.g., Rotunno et al. 1988; Weisman et al. 1988; Dudhia and Moncrieff 1989; Weisman 1992, 1993; Skamarock et al. 1994; Trier et al. 1997, 1998), radiative effects generally have not been considered, although Tucker and Crook (1999) recently simulated an MCS case with and without solar radiation. They found that the inclusion of solar radiative effects reduced the intensity of the MCS, although the details of how solar radiative effects were included were not presented.

Radiative effects also have virtually always been excluded from three-dimensional simulations of supercell storms, even though computing capabilities have advanced significantly since the seminal studies of the late 1970s and early 1980s (e.g., Wilhelmson and Klemp 1978; Rotunno and Klemp 1982; Klemp and Rotunno 1983). Some recent three-dimensional case study simulations of supercellular convection have included radiation, but these parameterizations have been rather crude. For example, often clouds were seen only as areas of very high water vapor content, with the radiative characteristics of condensed liquid and ice species not taken into account (e.g., Finley et al. 2001), leading to overestimates of solar fluxes reaching the surface in cloudy regions and underestimates of longwave cooling at cloud tops. Furthermore, to our knowledge, in the two- and three-dimensional simulations (of both MCSs and supercells) that have included radiation, no sensitivity analyses were done to quantify the effects of radiation on storm dynamics. The exclusion of radiative effects in the majority of convective storm simulation studies (particularly three-dimensional simulations) has been justified with the assumption that radiative processes are unimportant on the time scales of the model integration (e.g., Trier et al. 1997, 1998) and that the storms are “largely dynamically (not radiatively) driven” (Finley et al. 2001). Of course, all of the above statements are true in some sense, for the past modeling successes likely would not have been achieved otherwise. However, what we argue here, and what we are presently examining, is the possibility that convective storm dynamics may be modulated in certain, and perhaps significant, ways by radiative effects.

b. Observations of significant radiative effects attributable to long-lived convective storms

It is well known that low-level baroclinicity can have an important influence on convective storm dynamics. For example, low-level baroclinic zones (gust fronts) commonly are associated with the precipitation regions of convective storms. Klemp and Rotunno (1983) and Rotunno and Klemp (1985) showed that the forward-flank gust front of supercell thunderstorms (Lemon and Doswell 1979) may be an important source of horizontal vorticity for the updrafts of the storms. This horizontal vorticity is generated solenoidally along the boundary separating rain-cooled outflow from the relatively warm inflow. Large vertical velocity gradients associated with the updraft may tilt this horizontal vorticity to give rise to significant low-level vertical vorticity in supercell storms. It also has been shown that baroclinic boundaries associated with the precipitation
regions of other storms (e.g., adjacent storms or even storms occurring earlier in the day) may have similarly important dynamical consequences. For instance, when a storm crosses the outflow boundary left behind by some other region of convection, the storm may ingest enhanced baroclinic horizontal vorticity residing along the outflow boundary, which may lead to rapid intensification of low-level rotation (and often tornadogenesis), following tilting and stretching of the augmented horizontal vorticity (Purdom 1976; Maddox et al. 1980; Weaver and Nelson 1982; Markowski et al. 1998a; Atkins et al. 1999; Rasmussen et al. 2000). Even subtle low-level static stability changes not associated with horizontal temperature gradients are known to have significant impacts on storm behavior, and possibly even tornadogenesis (McCaul and Weisman 2001; Markowski et al. 2003).

Although the potential dynamical importance of low-level baroclinic zones associated with the precipitation regions of convection is well established, the dynamical significance of low-level baroclinic zones arising from radiative effects associated with convective storms have not been previously examined. Yet the magnitude of the low-level temperature perturbations and baroclinicity due to anvil-generated radiative effects has been found to be comparable to the magnitude of baroclinicity associated with storm-scale precipitation regions in at least some cases (e.g., Markowski et al. 1998b). This may not be entirely surprising. Even in stratiform precipitation events (e.g., those associated with cold-air damming), radiative effects have been found, at least in a few cases, to exert a greater influence on the low-level stability and horizontal temperature gradients than latent cooling associated with the evaporation of precipitation (e.g., Fritsch et al. 1992).

Markowski et al. (1998b) showed that baroclinic zones arising from surface cooling beneath optically thick anvil may be capable of generating horizontal vorticity of the same order of magnitude as that which is often generated along the more extensively studied gust fronts, and also of the same magnitude as the horizontal vorticity associated with the mean vertical wind shear of the ambient, large-scale environment \( O(10^{-2}) \) s\(^{-1} \). Such horizontal vorticity can be converted to vertical vorticity within storm updrafts via tilting, then amplified by stretching (Rotunno 1981; Davies-Jones 1984; Klemp 1987). Deep, persistent updraft rotation is the defining characteristic of supercell storms; thus, means of enhancing low-level horizontal vorticity may have important implications for the dynamics of such storms, in addition to the dynamics of other types of convective storms.

In the cases documented by Markowski et al. (1998b), temperature deficits as large as 5–6 K were found to develop within the anvil shadows. The temperature differences were observed to occur over horizontal distances of ~25 km. The rate at which horizontal vorticity is generated by such a baroclinic zone exceeds 0.02 s\(^{-1} \) h\(^{-1} \). The temperature gradients and associated vorticity generation rates owing to the anvil shadows may be smaller than temperature gradients often associated with the gust fronts of convective storms (~5 K km\(^{-1} \)). However, parcel residence times within anvil-generated baroclinic zones (Markowski et al. estimated the time scales to be ~1 h) would generally be larger than parcel residence times within the baroclinic zones associated with storm-scale gust fronts (~5–15 min) due to the larger horizontal scale of the anvil shadow compared to the scale of the precipitation region of the storm. Thus, the total horizontal vorticity generated baroclinically may be comparable to that produced by low-level outflow \( O(10^{-2}) \) s\(^{-1} \).

One question that Markowski et al. (1998b) were unable to fully address was the depth over which the cooling and baroclinicity developed. A few soundings indicated that the low-level baroclinicity was likely several hundred meters in depth. Although it is not known how deep the baroclinity must extend for significant dynamical effects to arise (this will be addressed by the research currently under way), there is growing evidence that modifications of just the lowest few hundred meters of the environmental vertical wind profile may have profound effects on storm behavior (Wicker 1996; Markowski et al. 1998c). Low-level temperature modifications by anvils also affect the convective available potential energy (CAPE) and convective inhibition (CIN) of the storm environment. It is not known what effects these alterations may have on convective storm behavior when included in a numerical simulation. Furthermore, it is not known how the effects of baroclinic vorticity differ depending on whether the baroclinic vorticity has been generated within a region in which equivalent potential temperature \( \theta_e \) has been nearly conserved (as might be expected to be the case along gust fronts where cooling is largely due to evaporation of precipitation) or whether the baroclinic vorticity has been generated within a region in which \( \theta_e \) deficits also have been generated (as might be expected to be the case where cooling owes to radiative effects). Even the forward speed of the convective storm might be expected to affect the magnitude of the radiative effects, at least those related to surface cooling due to a reduction of incident shortwave radiation. For example, a rapidly moving storm with its attendant anvil will constantly be encountering warm ground that it will have to cool in order to develop surface temperature
gradients. On the other hand, a stationary storm can shade the same ground for a longer period of time, thereby producing correspondingly larger surface temperature gradients. Conversely, the development of surface temperature gradients in storms due to low-level evaporative cooling is Galilean invariant since the precipitation region (which produces the cooling) moves with the storm.

3. Numerical simulations with emulated radiative cooling

Using version 4.5.2 of the Advanced Regional Prediction System (ARPS; Xue et al. 2000, 2001), we present a pair of preliminary simulations in order to illustrate the potentially important effects of radiative transfer processes on convective storm dynamics. The simulations are initialized with the composited sounding from the well-documented 20 May 1977 Del City, Oklahoma, storm (Ray et al. 1981; Johnson et al. 1987), which has been used in several other modeling studies (e.g., Klemp et al. 1981; Klemp and Rotunno 1983; Grasso and Cotton 1995; Adlerman et al. 1999; Adlerman and Droegemeier 2002). This sounding is characterized by a CAPE of approximately 2600 J kg$^{-1}$ and a 0–3 km storm-relative helicity of approximately 150 m$^2$ s$^{-2}$ (Fig. 1). The hodograph is shifted by a mean velocity so that the mature, cyclonically rotating storm is nearly stationary. One of the simulations (the control) is run without surface physics and radiation. In the other simulation, radiative cooling due to anvil shading is emulated by prescribing a cooling rate to the skin temperature of 5 K h$^{-1}$ at any grid point at which cloud water was present overhead. This skin cooling rate is similar to that observed by Markowski et al. (1998b). Low-level air temperatures are coupled to the skin cooling in this second simulation by the inclusion of surface sensible heat fluxes using simple bulk aerodynamic drag laws (latent and soil heat fluxes were not included). Though this emulation of radiative cooling is admittedly simple, it should suffice to illustrate the potential effects that radiative cooling under the anvil may have on storm dynamics.

The domain is 200 km$\times$ 200 km$\times$ 20 km, the horizontal grid spacing is 1000 m, and the vertical grid spacing varies from 150 m in the boundary layer to 500 m near the tropopause. Only warm-rain (Kessler) microphysics is used for both of the idealized simulations. Though this microphysical simplification is not necessary for our demonstration, we choose to use warm rain only for two reasons: computational expedience and, more importantly, neglecting ice processes leads to an anvil of smaller areal extent. Hence, if radiative cooling is important here, its importance will likely be ampli-
fied in the presence of a longer, thicker anvil. Neither simulation includes the Coriolis force.

The evolution of both simulations in the first hour is similar and will not be discussed in detail [see Klemp et al. (1981) for a more detailed discussion]. The initial updraft splits into anticyclonically (left moving) and cyclonically (right moving) rotating cells approximately 20 min into the simulations. The cyclonically rotating cell dominates throughout the rest of the simulations, becoming a mature supercell approximately after 40 min have elapsed. By about 60 min, the supercell takes on a nearly steady-state character in both simulations, with a persistent midlevel (3–7 km) mesocyclone and updrafts greater than 30 m s⁻¹.

The purpose of the simulations is to show that, beyond roughly the first 60 min, there are significant differences between the two supercells—differences that can only be due to effects associated with the emulated anvil shading. Our goal is not to present detailed diagnostics of the model output here, elucidating the precise dynamics responsible for the simulation differences, for this is one of the goals of our future research. Our goal here is only to show that radiative effects associated with cirrus anvils can have a significant impact on convective storm characteristics.

The differences between the two simulations do not become significant until after approximately an hour has elapsed (Figs. 2, 3, and 4) by which time a well-developed anvil is present (Fig. 2). In the simulation having emulated cloud shading, near-ground air temperature deficits beneath the anvil outside of the forward-flank precipitation region of up to 3 K (4 K) develop by t = 2 h (t = 3 h). These deficits are similar in amplitude to those observed by Markowski et al. (1998b). Consistent with the prescribed skin cooling rate of 5 K h⁻¹ beneath clouds, skin temperature deficits of approximately 8 K (13 K) develop by t = 2 h (t = 3 h; Fig. 5a). The minimum surface sensible heat flux beneath the anvil is approximately −450 W m⁻² (Fig. 5b), which seems reasonable given that observed net radiation decreases of ∼500 W m⁻² have been observed with the passage of optically thick anvils associated with severe storms (Markowski et al. 1998b). The depth of the cooling (Fig. 6) is approximately 500 m, which also is similar to the observations documented by Markowski et al. (1998b). The similarity of the horizontal air temperature fields, vertical temperature profiles, and sensible heat fluxes to those that have been observed beneath anvils provide some confidence that the simple cloud shading parameterization has produced at least a qualitatively realistic temperature field beneath the anvil.

Although the temperature deficits may be considered small and shallow compared to those frequently found in the precipitation-induced convective outflows of simulated storms (often >8 K), the expansive region of surface cooling in the storm inflow has an effect on subsequent storm morphology and evolution that may be regarded as substantial. For example, the time series of maximum vertical velocity and low-level vertical vorticity (Fig. 4) have differences as large as 20% (100%) at some times. The rainwater fields also have obvious differences by t = 3 h (Figs. 3c and 3f).¹

The supercell simulated without radiative effects generally has much stronger low-level rotation and a more occluded gust-front structure compared to the supercell simulated with emulated cloud shading (Figs. 3 and 4). In fact, the differences in the near-surface vector wind fields in the simulated storms are much larger than those that have been observed between tornadic and nontornadic supercells (Blanchard and Straka 1998; Trapp 1999; Wakimoto and Cai 2000; Markowski et al. 2002). The low-level potential temperature fields, especially the orientation and magnitude of the gradients in close proximity to the storms, have readily discernible differences; thus, it is not surprising that large kinematic differences (e.g., the vertical vorticity differences) arise, given the well-known relationship between temperature gradients, horizontal vorticity modulation, and vertical vorticity generation by tilting.

4. Discussion

We reiterate that a detailed investigation of the dynamical causes for the differences between the two simulations described in section 2 is beyond the scope of this preliminary report, but that the results displayed in Figs. 3 and 4 quite clearly indicate that substantial modifications of storm behavior can be brought about by radiative processes. In this pair of example simula-

¹ An additional control simulation was conducted in which radiation was excluded but a surface sensible heat flux was included. Although the surface energy budget was somewhat unrealistic, the experiment was conducted in order to address concerns that the differences between the simulations with and without radiation and surface physics might be due largely to the presence of a surface sensible heat flux rather than radiative cooling in the cloud shadow. Although some differences were observed between the two control simulations, the differences between each control simulation and the simulation that included radiation were considerably larger. Thus, the differences between the original control simulation and the simulation that included radiation and surface physics are much more strongly a consequence of the radiative cooling of the shaded ground (coupled to the air temperature by the sensible heat flux) than simply a consequence of the inclusion of the sensible heat flux.
It appears as though low-level cooling beneath the anvil has had a detrimental effect on the convective storm. In other cases, (e.g., cases in which the orientation of the low-level inflow with respect to the low-level baroclinity is more favorable), it is quite possible that anvils could have an enhancing effect on a convective storm. The research that is currently under way is designed to determine precisely the situations in which radiation has a significant effect on convective storms, as well as to determine whether the effects are positive or negative and what is the dynamical nature of the effects.

A few additional comments are in order concerning the demonstration simulations. The long-lived supercell
Fig. 3. (a)–(c) Horizontal cross sections of the rainwater (3 km), potential temperature perturbation (75 m), and vertical vorticity (75 m) fields at $t = 1$ h, $t = 2$ h, and $t = 3$ h, respectively, in the simulation in which no radiative parameterization was employed. The region shown is indicated in Fig. 2a. Light (dark) gray shading denotes regions where rainwater exceeds $1 \text{ g kg}^{-1}$ ($3 \text{ g kg}^{-1}$). The vertical vorticity field is analyzed at 0.004 $s^{-1}$ intervals using bold contours (negative contours are dashed). Negative potential temperature perturbations are analyzed at 1-K intervals using thin, dashed contours. Horizontal (ground relative) wind velocity vectors at 75 m have been drawn at every third grid point. (d)–(f) Same as in (a)–(c) but for the simulation in which shortwave radiative cooling was emulated beneath cloud regions. The region shown is indicated in Fig. 2d.
storms simulated in the pair of demonstration simulations are nearly stationary. Thus, it might seem that the simulation with emulated radiative cooling perhaps exaggerates the effect of anvil shading due to shading of the same region for a long duration. However, the surface temperature deficit and associated horizontal baroclinity beneath the anvil, even after 3 h (not shown), are not as large as has been observed. Furthermore, the hodograph structure (Fig. 1) is not ideal—not only did low-level inflow parcels fail to spend much time in the anvil-generated baroclinic zone, but the baroclinic zone itself was situated so that inflow entering the updraft did not pass through the (southern) portion of the baroclinic zone that would have augmented the horizontal vorticity associated with the base-state vertical wind shear. Instead, the horizontal

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**Fig. 4.** Time series of (left) maximum vertical velocity, $w_{\text{max}}$ (m s$^{-1}$), and (right) maximum vertical vorticity below 2 km, $\zeta_{\text{max}}$ ($\times10^3$ s$^{-1}$), in the demonstration simulations without radiative effects (solid) and with emulated anvil radiative effects (dashed).

**Fig. 5.** (a) Horizontal cross sections of the rainwater (3 km) and skin temperature fields at $t = 2$ h in the simulation in which shortwave radiative cooling was emulated beneath cloud regions. The region shown is indicated in Fig. 2d. Light (dark) gray shading denotes regions where rainwater exceeds 1 g kg$^{-1}$ (3 g kg$^{-1}$). The skin temperature field is analyzed at 2-K intervals. Horizontal (ground relative) wind velocity vectors at 75 m have been drawn at every third grid point. (b) Horizontal cross sections of the rainwater (3 km) and sensible heat flux fields at $t = 2$ h in the same simulation. The sensible heat flux field is analyzed at 100 W m$^{-2}$ intervals (negative contours are dashed).
vorticity produced by the anvil-generated baroclinic zone actually opposed the horizontal vorticity associated with the base-state vertical wind shear. Perhaps this is why the radiatively modified storm had weaker near-surface rotation, or perhaps there are other reasons (e.g., increased CIN in the inflow) that will be discovered upon completing diagnostics of future experiments using a more complete radiation parameterization. It is also worth noting that the demonstration simulations do not include ice physics. The inclusion of ice physics leads to the production of more expansive anvils (and therefore more expansive surface temperature modifications) compared to the warm-rain microphysical parameterization used for the demonstration simulations (Gilmore and Wicker 1998). Given the above-noted departures from what might be considered to be much more ideal conditions for magnifying the importance of anvil radiative effects on convective storms, we believe that the demonstration simulations quite conservatively indicate that radiative effects can have important effects on convective storms.

It does not seem likely that radiative effects would be important in all convective storms. For example, short-lived storms probably would not be affected by radiatively cooled shadow regions, owing to their relatively brief duration and small anvils. On the other hand, long-lived storms might be more prone to radiative effects on their dynamics, owing to their larger anvil canopies and longer storm time scales. Furthermore, long-lived storms tend to occur in environments containing large vertical wind shear, which promotes storm organization and longevity. Large vertical wind shear typically is associated with strong storm-relative winds at anvil level, leading to the formation of long anvils in the downstream direction, overlying the storm inflow region where surface shading effects may have the largest impact. Also, the most dangerous convective storms are often isolated (Browning 1964), and thus may have a well-defined anvil shadow edge and associated low-level baroclinity.

5. Future work

The preliminary work summarized herein represents the first step of a larger effort to explore the effects of radiative transfer processes on isolated convective storms. Our next step is to include more sophisticated radiative and microphysical parameterizations in a series of simulations designed to establish bounds on the magnitude of radiative effects on long-lived convective storms, as well as the nature of these effects and how these effects depend on storm morphology and the ambient environment. Since all radiation codes that are used in operational forecast and cloud models are one dimensional (1D), they only account for clouds that are overhead. Consequently, true three-dimensional shadowing effects are not possible. We plan to modify an existing 1D radiation code so that 3D shadowing effects are approximately accounted for by modifying the solar direct beam. Since the direct (as opposed to diffuse) radiative fluxes are the primary reason for the shadowed region, it should be straightforward to modify the attenuation of the solar direct beam so that it accounts for both solar zenith and azimuth (i.e., 3D) effects.

Fig. 6. (a) Model sounding beneath the anvil at $t = 2$ h at the location indicated by the star in Fig. 2c. The base-state temperature profile is indicated with the dashed line. (b) Observed sounding beneath the anvil of a thunderstorm complex on 8 Jun 1995. (c) Visible satellite image from 2315 UTC 8 Jun 1995. The star indicates the location of the sounding shown in (b).
results of these experiments will be reported in forthcoming articles.

Acknowledgments. We thank the anonymous reviewers and Drs. Jerry Straka and Erik Rasmussen for constructive suggestions during the course of our work. This research was partially supported by the National Science Foundation (Grant ATM-0338661). J. Harrington was supported by the Office of Science (BER), U.S. Dept. of Energy, Grant DE-F602-05ER64058.

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